

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



General Certificate of Education
Advanced Level Examination
June 2014

Mathematics

MFP3

Unit Further Pure 3

Monday 19 May 2014 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



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QUESTION
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- 3 A curve has polar equation $r(4 - 3 \cos \theta) = 4$. Find its Cartesian equation in the form $y^2 = f(x)$.

[4 marks]

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4 Solve the differential equation

$$\frac{d^2y}{dx^2} - 2\frac{dy}{dx} - 3y = 2e^{-x}$$

given that $y \rightarrow 0$ as $x \rightarrow \infty$ and that $\frac{dy}{dx} = -3$ when $x = 0$.

[10 marks]

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7 (a) It is given that $y = \ln(\cos x + \sin x)$.

(i) Show that $\frac{d^2y}{dx^2} = -\frac{2}{1 + \sin 2x}$.

[4 marks]

(ii) Find $\frac{d^3y}{dx^3}$.

[1 mark]

(b) (i) Hence use Maclaurin's theorem to show that the first three non-zero terms in the expansion, in ascending powers of x , of $\ln(\cos x + \sin x)$ are $x - x^2 + \frac{2}{3}x^3$.

[3 marks]

(ii) Write down the first three non-zero terms in the expansion, in ascending powers of x , of $\ln(\cos x - \sin x)$.

[1 mark]

(c) Hence find the first three non-zero terms in the expansion, in ascending powers of x , of $\ln\left(\frac{\cos 2x}{e^{3x-1}}\right)$.

[4 marks]

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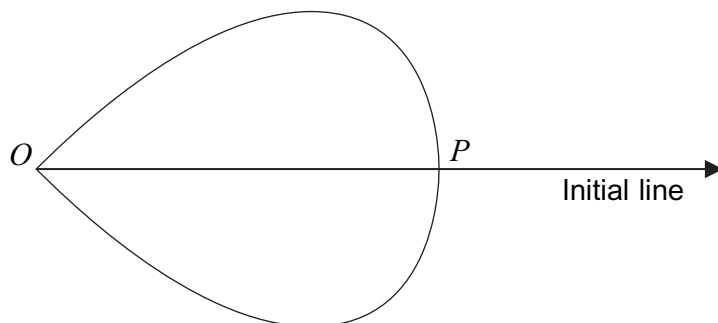
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- 8 The diagram shows a sketch of a curve C , the pole O and the initial line. The curve C intersects the initial line at the point P .



The polar equation of C is $r = (1 - \tan^2 \theta) \sec \theta$, $-\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$.

- (a) Show that the area of the region bounded by the curve C is $\frac{8}{15}$. **[5 marks]**

- (b) The curve whose polar equation is

$$r = \frac{1}{2} \sec^3 \theta, \quad -\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$$

intersects C at the points A and B .

- (i) Find the polar coordinates of A and B . **[3 marks]**

- (ii) Given that angle $OAP = \text{angle } OBP = \alpha$, show that $\tan \alpha = k\sqrt{3}$, where k is an integer. **[4 marks]**

- (iii) Using your value of k from part (b)(ii), state whether the point A lies inside or lies outside the circle whose diameter is OP . Give a reason for your answer. **[1 mark]**

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END OF QUESTIONS

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